## Solution I

## Question 1

a) The stem-and-leaf display of the scores is

| 9 | 58 |
| ---: | :--- |
| 10 | 6 |
| 11 | 559 |
| 12 | 6 |
| 13 | 135678 |
| 14 | 344557 |
| 15 | 2478 |
| 16 | 01222567 |
| 17 | 14688 |
| 18 | 24 |
| 19 | 04 |

b) The sample mean is $=6005 / 40=150.125$
c) Median $=(152+154) / 2=153$
d) $40 / 4=10$, so we need to count in 10 observations. The $11^{\text {th }}$ smallest observation also satisfies the definition. This yields $Q_{1}=\frac{135+167}{2}=135.5$

Using a similar approach, we find that $Q_{3}=\frac{166+167}{2}=166.5$
e) Interquartile range $=Q_{1}-Q_{3}=166.5-135.5=31.0$ points

## Question 2

a) In the following frequency distribution of lizard speed (in meters per second), the left endpoint is included in the class interval but not the right endpoint.

| Class Interval | Frequency | Relative Frequency |
| :--- | :---: | :---: |
| 0.45 to 0.90 | 2 | 0.067 |
| 0.90 to 1.35 | 6 | 0.200 |
| 1.35 to 1.80 | 11 | 0.367 |
| 1.80 to 2.25 | 5 | 0.167 |
| 2.25 to 2.70 | 6 | 0.200 |
| Total | 30 | 1.001 (rounding error) |

b) All of the class intervals are of length 0.45 so we can graph rectangles whose heights are the relative frequency. The histogram is

c) The ordered data are

$$
\begin{array}{lllllllll}
0.50 & 0.76 & 1.02 & 1.04 & 1.20 & 1.24 & 1.28 & 1.29 & 1.36 \\
1.49 \\
1.55 & 1.56 & 1.57 & 1.57 & 1.63 & 1.70 & 1.72 & 1.78 & 1.78 \\
1.92 \\
1.94 & 2.10 & 2.11 & 2.17 & 2.47 & 2.52 & 2.54 & 2.57 & 2.66 \\
2
\end{array} .67
$$

Since the number of observations is 30 , the median or second quartile is the average of the $15^{\text {th }}$ and $16^{\text {th }}$ in the list. Sample median $=(1.63+1.70) / 2=1.665$ meters per second. Because $30 / 4=7.5$, the first quartile is the $8^{\text {th }}$ ordered observation, and because $(0.75)(30)=22.5$, the third quartile is the $23^{\text {rd }}$ ordered observation:

$$
Q_{1}=1.29 \quad Q_{2}=1.665 \quad Q_{3}=2.11
$$

d) Since $0.9(30)=27$, the $90^{\text {th }}$ percentile is the average of the $27^{\text {th }}$ and $28^{\text {th }}$ observation in the ordered list. Sample $90^{\text {th }}$ percentile $=(2.54+2.57) / 2=2.555$.

## Question 3

a. $\bar{x}=6.78$ and $s=\sqrt{19.4096}=4.406$
b. Sample median $=(6+7) / 2=6.5$. Both the sample mean and the sample median give a good indication of the amount of mineral lost.

|  |  | $\bar{x} \pm s$ | $\bar{x} \pm 2 s$ | $\bar{x} \pm 3 s$ |
| :--- | ---: | :--- | :---: | :--- |
| c. | Interval: | $(2.369,11.181)$ | $(2.037,15.587)$ | $(-6.443,19.993)$ |
|  | Proportion: | $26 / 40=0.65$ | $38 / 40=0.95$ | $40 / 40=1.00$ |
|  | Guidelines: | 0.68 | 0.95 | 0.997 |

d. We observe a good agreement with the proportions suggested by the empirical guideline.

